

## Common Core Algebra II

### MRS21 Course Overview (Tentative)

Unit #1	Algebraic Expressions and Operations on Polynomials
Total: 6 days	<ul style="list-style-type: none"><li>• Lesson #1: Classifying Polynomials and Evaluating Expressions</li><li>• Lesson #2: Operations on Polynomials (addition, subtraction, multiplication)</li><li>• Lesson #3-4: Special Polynomial Identities</li><li>• Lesson #5-6: Binomial Expansion</li></ul>

Unit #2	Functions and Their Characteristics
Total: 9 days	<ul style="list-style-type: none"><li>• Lesson #1: Introduction to Non-Linear Functions</li><li>• Lesson #2: Function Notation and Composition of Functions</li><li>• Lesson #3: Domain and Range of a Function</li><li>• Lesson #4: Inverses of Linear Functions</li><li>• Lesson #5: Key Features of Functions</li><li>• Lesson #6: Solving Systems of Equations Graphically (involving higher degree equation given in function notation, discuss 3 cases, use calculator)</li><li>• Lesson #7-9: System of Three Linear Equations</li></ul>

Unit #3	Quadratic Functions and Their Algebra
Total: 14 days	<ul style="list-style-type: none"><li>• Lesson #1: Review of Factoring Methods(GCF, trinomial, special binomials)</li><li>• Lesson #2: Factoring Completely</li><li>• Lesson #3: Factoring by Grouping</li><li>• Lesson #4: Equivalence of Expressions and Functions (see #5, 20 august, #8, #31 june)</li><li>• Lesson #5: Quadratic Function Review</li><li>• Lesson #6: Completing the Square and Shifting Parabolas</li><li>• Lesson #7: Intercept Form of Quadratic Function</li><li>• Lesson #8: Solving Quadratics Using Zero Product Rule</li><li>• Lesson #9: Modeling with Quadratic Functions</li><li>• Lesson #10: Solving Systems Involving Lines, Circles, and Parabolas Algebraically (see #33 june)</li><li>• Lesson #11: The Locus Definition of a Parabola</li><li>• Lesson #12-13: Equation of Parabola with Vertex not at the Origin (Horizontal and Vertical Shift)</li><li>• Lesson #14: Writing Equation of Parabola Using Locus Definition</li></ul>

Unit #4	Complex Numbers
Total: 5 days	<ul style="list-style-type: none"><li>• Lesson #1: Imaginary Number</li><li>• Lesson #2: Simplifying Powers of <math>i</math> and intro to Complex Numbers</li><li>• Lesson #3: Operations on Complex Numbers (#27 august)</li><li>• Lesson #4: Solving Quadratic Equations with Complex Solutions</li><li>• Lesson #5: The Discriminant and the Nature of the Roots</li></ul>

Unit #5	Polynomial Functions and their Algebra
Total: 11 days	<ul style="list-style-type: none"> <li>• Lesson #1: Long Division of Polynomials</li> <li>• Lesson #2: Synthetic Division of Polynomials</li> <li>• Lesson #3: Application of Synthetic Division of Polynomials</li> <li>• Lesson #4: Remainder and Factor Theorem</li> <li>• Lesson #5: Solving Higher Degree Polynomial Equations</li> <li>• Lesson #6: Writing Equations of Higher Degree Polynomial Functions given their roots</li> <li>• Lesson #7: Graphs and Zeros of Polynomial Functions</li> <li>• Lesson #8-9: Sketching the Graphs of Polynomial Functions</li> <li>• Lesson #10: Even and Odd Functions</li> </ul>

Unit #6	Rational Expressions and Equations
Total: 7 days	<ul style="list-style-type: none"> <li>• Lesson #1: Simplifying Rational Expressions</li> <li>• Lesson #2: Multiplying and Dividing Rational Expressions</li> <li>• Lesson #3-4: Adding and Subtracting Rational Expressions (#17 august)</li> <li>• Lesson #5: Complex Fractions</li> <li>• Lesson #6: Solving Rational Equations</li> <li>• Lesson #7: Applications of Rational Equations</li> </ul>

Unit #7	Powers and Radicals
Total: 7 days	<ul style="list-style-type: none"> <li>• Lesson #1: Review of Integer Exponents</li> <li>• Lesson #2: Fractional Exponents</li> <li>• Lesson #3: Properties of Exponents and Radicals</li> <li>• Lesson #4: Simplifying Radical Expressions (#26 august)</li> <li>• Lesson #5: Solving Square Root Equations</li> <li>• Lesson #6: Solving Cube Root, Forth Root Equations, and Equations with Fractional Exponents</li> <li>• Lesson #7: EXTENSION Graphing Square Root and Cube Root Functions</li> </ul>

**Total: 59 lessons.**

On-line resources:

1. eMath instruction lessons: <http://emathinstruction.com/common-core-algebra-ii-all-units-first-draft/>
2. LearnZillion – CC Standards with aligned on-line lessons: [https://learnzillion.com/common\\_core/math/algebra](https://learnzillion.com/common_core/math/algebra)
3. Mathbitsnotebook:

## Unit #1: Algebraic Expressions and Linear Functions

- Lesson #1: Classifying Polynomials and Evaluating Expressions

Standards		
Objectives	<ul style="list-style-type: none"> <li>State the degree of a polynomial and the number of terms in a polynomial</li> <li>Add and subtract expressions with multivariable terms like <math>-13x^2y^4</math></li> <li>Evaluate expressions with multivariable terms</li> <li>Add and subtract polynomials</li> </ul> <p>EXTENSION: (see Engage NY Lesson #1 Mod #1)</p> <ul style="list-style-type: none"> <li>Determine the 1<sup>st</sup>, 2<sup>nd</sup>, and 3<sup>rd</sup> difference of any second degree or third degree polynomial (n-th degree polynomial will have a constant n-th difference)</li> <li>Determine the degree of a polynomial given the table of values generated by a polynomial)</li> </ul>	
Resources	Amsco: p.6-8, p.133-137	eMath: Unit #1 lesson #1 Engage NY: Lesson #1 Mod #1

- Lesson #2: Multiplying Polynomials

Standards	A-SSE.A.2 & A-APR.C.4 Practice MP.7 & MP.8	
Objectives	<ul style="list-style-type: none"> <li>Multiply binomials, trinomials, and higher degree polynomials using distributive method</li> <li>Use distributive property to prove useful identities such as:  <math>(a + b)^2 = a^2 + 2ab + b^2</math>,  <math>(x^n - y^n)(x^n + y^n) = x^{2n} - y^{2n}</math>, including <math>(x - y)(x + y) = x^2 - y^2</math> and  <math>(x^2 - y^2)(x^2 + y^2) = x^4 - y^4</math></li> </ul> <p>EXTENSION: Multiply polynomial using area model (tabular method)</p>	
Resources IMG 1185	Amsco: p.39 – 40, p.137 Assessment Readiness p.27	eMath: Unit #1 lesson #4, 5 EngageNY: Mod #1 Lesson # 2

- Lesson #3: Special Polynomial Identities

Standards	A-SSE.A.2, A-APR.C.4, & Practice MP.7	
Objectives	<ul style="list-style-type: none"> <li><b>((including more difficult cases, see #5, 20 august )</b></li> <li>Use the structure of an expression to identify ways to rewrite it. <i>For example, see <math>x^4 - y^4</math> as <math>(x^2)^2 - (y^2)^2</math>, thus recognizing it as a difference of squares that can be factored as <math>(x^2 - y^2)(x^2 + y^2)</math></i></li> <li>use the perfect square binomial identity <math>(x - y)^2 = x^2 - 2xy + y^2</math> on more complex problems</li> <li>Use sum and difference of cubes identities</li> </ul> <p>EXTENSION: Use the polynomial identity <math>(x^2 - y^2)^2 + (2xy)^2 = (x^2 + y^2)^2</math> to state Pythagorean triples and their multiples (NOTE: students do need to memorize it, just how to use it)</p>	
Resources	Amsco: p.80-88, 93 See assessment readiness questions	eMath: unit # 10 lesson #4 Engage NY: Mod #1 Lesson #2, #10

## Unit #2: Functions and Their Characteristics

- Lesson #1: Introduction to non-Linear Functions

Standards	MP. 8. Look for and express regularity in repeated reasoning. F-IF.1
Objectives	<ul style="list-style-type: none"> <li>Identify independent and dependent variable</li> </ul>

	<ul style="list-style-type: none"> <li>Determine whether relation is a function using the vertical line test</li> <li>Determine if a function is one-to-one (horizontal line test) or onto</li> <li>Distinguish between different types of functions (linear, quadratic, absolute value, square root, exponential) given their equations and/or graphs</li> </ul>	
Resources	Amsco: p.48 - 49	eMath: Unit #2 lesson #1, lesson #5 Engage NY:

• Lesson #2: Function Notation and Composition of Functions

Standards	F-IF.1, F-IF.2	
Objectives	<ul style="list-style-type: none"> <li>Recognize and interpret different function notations</li> <li>Given <math>f(x)</math> (linear or quadratic), find <math>f(x-a)</math> or <math>f(x+a)</math> where 'a' is rational number</li> <li>Evaluate a given function for a given value</li> <li>Given equations of functions, find composition of functions using two different notations <math>f(g(x))</math> or <math>f \circ g(x)</math></li> <li>Find composition of functions using graphs of functions</li> </ul>	
Resources	Amsco: p.22-24,	eMath: Unit #2 lesson #2, lesson #3 Engage NY:

• Lesson #3: Domain and Range of a Function

Standards	F-IF.1, F-IF.5	
Objectives	<ul style="list-style-type: none"> <li>Use set builder or interval notation to represent domain and range of a function given its graph</li> <li>Given the graph of a function and a value of the domain, find the corresponding value of range</li> <li>Find range given domain and an equation of linear or quadratic function</li> <li>Find restricted domain and range of rational and radical functions</li> </ul>	
Resources	Amsco:	eMath: unit #2 lesson 4 Engage NY:

• Lesson #4: Inverses of Linear Functions

Standards	F-BF.4	
Objectives	<ul style="list-style-type: none"> <li>Define inverse of a function</li> <li>Find inverse of a linear function algebraically (in a slope-intercept form or point-slope form) and graphically</li> <li>Find inverse of different functions given a table of values, an equation, or a graph</li> <li>Explore the inverse relationship of linear functions using graphing calculator</li> </ul> <p>EXTENSION: find an inverse of cubic and square root functions</p>	
Resources	Amsco: p.281-285 Pearson: 409-410	eMath: Unit #2 lesson #6, Unit #3 lesson #5

• Lesson #5: Key Features of Functions

Standards	F-IF.4	
Objectives	<ul style="list-style-type: none"> <li>Given a graph or an equation, identify x and y-intercepts of the function</li> <li>State zeros of a function given its graph</li> <li>State relative and absolute minimum and maximum of a function</li> <li>Identify increasing and decreasing intervals of a function</li> <li>State when function is positive (<math>f(x) &gt; 0</math>) or negative (<math>f(x) &lt; 0</math>)</li> <li>(end behavior notation)</li> </ul>	
Resources	Amsco:	eMath: unit #2 lesson #7 Engage NY:

--	--	--

• Lesson #6: Solving Systems of Equations Graphically

Standards	F-IF.4	
Objectives	<ul style="list-style-type: none"> <li>(involving higher degree equation given in function notation, discuss 3 cases, use calculator)</li> <li></li> </ul>	
Resources	Amsco:	eMath: unit #2 lesson #7 Engage NY:

• Lesson #7-8: System of Three Linear Equations

Standards	MP 7. Look for and make use of structure. MP 1. Make sense of problems and persevere in solving them.	
Objectives	( #23 august, algebraically, calculator, application) <ul style="list-style-type: none"> <li>Solve system of linear equations with three variable by using elimination or substitution</li> <li>Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.</li> <li>EXTENSION: Given three points of the parabola, write a quadratic equations for this function</li> </ul>	
Resources	Amsco: p.72-74	eMath: Unit #3 lesson #7 Engage NY: Mod 1 lesson #30

**Unit #3: Quadratic Functions and Their Algebra**

• Lesson #1: Review of Factoring Methods

Standards	N-Q.A.2, A-SSE.A.2, A-APR.B.2, A-APR.B3, A-APR.D.6, F-IF.C.7c. MP 7: Look for and make use of structure	
Objectives	<ul style="list-style-type: none"> <li>Factor using GCF</li> <li>Factor using the difference of two perfect squares</li> <li>Factor quadratic trinomials with leading coefficient 1</li> <li>Factor perfect square trinomials</li> </ul>	
Resources	Amsco: p.79 - 80	eMath: unit #6 lesson #2 Engage NY:

• Lesson #2: Factoring Completely

Standards	N-Q.A.2, A-SSE.A.2, A-APR.B.2, A-APR.B3, A-APR.D.6, F-IF.C.7c	
Objectives	<ul style="list-style-type: none"> <li>Examine the structure of a polynomial to identify the most appropriate factoring method</li> <li>Factor more complex difference of perfect squares and perfect square trinomials</li> <li>Factor polynomials completely</li> <li>Apply factoring strategies to solve a real-world problem</li> </ul> EXTENTION: <ul style="list-style-type: none"> <li>Factor polynomials with a binomial common factor. Ex: <math>x^2(2x + 1) - 4(2x + 1)</math></li> <li>Factor the difference of perfect cubes</li> </ul>	
Resources	Amsco: p.80 – 83, 85 IMG 1227	eMath: unit #6 lesson #4 Engage NY: Mod #1 Lesson #13

- Lesson #3: Factoring by Grouping

Standards	A-REI.4.b	
Objectives	<ul style="list-style-type: none"> <li>Factoring four-term polynomials by identifying a common binomial factor (by grouping)</li> <li>Factoring quadratic trinomials with <math>a &gt; 1</math> by grouping</li> </ul>	
Resources	Amsco: p.84, 88	eMath: unit #6 lesson #5 Engage NY: Mod #1 Lesson #12, 13

- Lesson #4: Equivalence of Expressions and Functions

Standards	MP 7. Look for and make use of structure. MP 1. Make sense of problems and persevere in solving them.	
Objectives	<ul style="list-style-type: none"> <li>Use polynomial identities to show that two expressions are equivalent</li> <li>Use polynomial identities to prove that an equation is an identity</li> </ul>	
Resources	Amsco: p.72-74	eMath: Unit #3 lesson #7 Engage NY: Mod 1 lesson #30

- Lesson #4: Quadratic Function Review (standard form, axis of symmetry, vertex, intercepts)

Standards	F-IF.4, F-IF.7.a	
Objectives	<ul style="list-style-type: none"> <li>Sketch parabola given its equation in a standard form</li> <li>Find main characteristics of a parabola such as turning point (vertex), axis of symmetry, and x and y-intercepts</li> <li>State domain and range of a given quadratic</li> <li>Indicate the interval on which the function is positive or negative, increasing and decreasing</li> </ul>	
Resources	Amsco:	eMath: unit #6 lesson #1 Engage NY:

- Lesson #5: Completing the Square and Shifting Parabolas (getting parabola to vertex form and analyzing the shift of a vertex)

Standards	F-IF.8.a, F-BF.3	
Objectives	<ul style="list-style-type: none"> <li>Rewrite quadratic equation from standard form to a vertex form</li> <li>Given the vertex form of the equation state the turning point</li> <li>Introduce transformation notation of a function <math>af(x-h)+k</math> and analyze the horizontal and vertical shift of a vertex of a parabola</li> </ul> <p>EXTENSION:</p> <ul style="list-style-type: none"> <li>Compare completing a square method to other methods of solving quadratics</li> </ul>	
Resources	Amsco: p.42-43	eMath: unit # 6 lesson #8 Engage NY: Mod #1 Lesson # 35

- Lesson #6: Intercept Form of Quadratic Function

Standards	F-IF.8.a, F-BF.3	
Objectives		
Resources	Amsco:	eMath:

• Lesson #7: Solving Quadratics Using Zero Product Rule

Standards	A.APR.B.3, F-IF.8.a	
Objectives	<ul style="list-style-type: none"> <li>Solving quadratics by factoring, including factoring by grouping</li> <li></li> <li>Writing equation of quadratic by identifying the roots from the graph and working backwards</li> </ul>	
Resources	Amsco: p.89-91	eMath: unit #6 lesson #6 Engage NY:

• Lesson #8: Modeling with Quadratic Functions

Standards	F-IF.8.a, F-IF.9, F-IF.4, F-IF.5	
Objectives	<ul style="list-style-type: none"> <li>Real world application of quadratic function (finding maximum height, time an object lasts in the air, etc.)</li> <li>Create a graph of a quadratic using appropriate scale related to a given word problem</li> <li>Explain the meaning of x and y-intercepts in the context of the problem</li> <li>Use graphing calculator</li> </ul>	
Resources	Amsco: Big Ideas: Chapter 2.4	eMath: unit #6 lesson #9 Engage NY:

• Lesson #9: Systems Involving Lines, Circles, and Parabolas

Standards	A-REI.7	
Objectives	<ul style="list-style-type: none"> <li>Review of distance formula and general equation of a circle</li> <li>Solving systems of linear-circular, circular-parabolic equations graphically</li> <li>Solve algebraically and graphically a system of linear-quadratic equations</li> </ul>	
Resources	Amsco: p.175-178	eMath: unit #6 lesson #10 Engage NY: Mod 1 lesson #31, 32

• Lesson #10: The Locus Definition of a Parabola

Standards	G-GPE.A.2, F-EF.8	
Objectives	<ul style="list-style-type: none"> <li>Define directrix and focus of a given parabola</li> <li>Use analytic equation of a parabola <math>y = \frac{1}{4p}x^2</math> or <math>x = \frac{1}{4p}y^2</math> to determine if it opens up, down, left or right</li> <li>Write an equation of a parabola centered at the origin and with a given focus</li> <li>Identify vertex, focus, and directrix of a parabola given its equation</li> <li>Create a sketch of a parabola given its equation in the above described forms</li> <li>Write an equation of a parabola given directrix and focus</li> </ul>	
Resources	Amsco: p. 118-125    Pearson: 622 - 625 Big Ideas: Chapter 2.3	eMath: unit #6 lesson #11 Engage NY: mod 1 lesson #33, 34 Pearson: p.622

• Lesson #11-12: Equation of Parabola with Vertex not at the Origin

Standards	G-GPE.A.2	
Objectives	<ul style="list-style-type: none"> <li>Represent vertical and horizontal shifts of a parabola with an appropriate analytic equation in the form of <math>(x - h)^2 = 4p(y - k)</math>, <math>(y - k)^2 = 4p(x - h)</math></li> <li>Find the vertex, focus, and directrix of a given parabola in the above mentioned form</li> <li>Match equation of the parabola in analytic form with its corresponding graph</li> <li>Find vertex of a parabola given its analytic equation</li> </ul>	

Resources	Amsco: p. 118-125    Pearson: 626-629 Assessment Readiness: p.101 -102	eMath: unit #6 lesson #11 Engage NY: mod 1 lesson #33, 34 Pearson: p.626
-----------	---	--

• Lesson #13: Writing Equation of Parabola Using Locus Definition

Standards	G-GPE.A.2	
Objectives	<ul style="list-style-type: none"> <li>Write an equation of a parabola with given vertex and focus</li> <li>Write an equation of a parabola with given vertex and directrix</li> <li>Write equation of a directrix given focus and vertex</li> <li>Find the equation of the set of points which are equidistant from a given point and a directrix (example: point (4, -2) and the line <math>y=4</math>) . Sketch this set of points</li> </ul> <p>EXTENSION:</p> <ul style="list-style-type: none"> <li>Write an analytic equation of a parabola given its graph</li> </ul>	
Resources	Amsco: p. 118-125	eMath: unit #6 lesson #11 Engage NY: mod 1 lesson #33, 34

**Unit #4: Complex Numbers**

• Lesson #1: Imaginary Number

Standards	N-CN.A.1, N-CN.A.2, N-CN.C.7, MP 8. Look for and express regularity in repeated reasoning.	
Objectives	<ul style="list-style-type: none"> <li>State the definition of the imaginary unit <math>i</math> and pure imaginary numbers</li> <li>Simplifying radicals with the negative radicands</li> <li>Solve incomplete quadratics which lead to imaginary roots</li> <li>Simplifying powers of <math>i</math></li> </ul>	
Resources	Amsco: p.103-105	eMath: unit #9 lesson #1 Engage NY: Mod #1 Lesson #37

• Lesson #2: Operations on Complex Numbers

Standards	N-CN.A.1, N-CN.A.2, N-CN.A.4, N-CN.C.7	
Objectives	<ul style="list-style-type: none"> <li>Adding and subtracting complex numbers</li> <li>Finding conjugates of complex numbers</li> <li>Multiplying complex numbers</li> </ul> <p>Extension: Graph complex numbers on a complex plane</p>	
Resources	Amsco: p. 103-105	eMath: unit #9 lesson #2 Engage NY: Mod #1 Lesson #38

• Lesson #3: Solving Quadratic Equations with Complex Solutions

Standards	N-CN.C.7, A-REI.B.4b	
Objectives	<ul style="list-style-type: none"> <li>Solve quadratic equations with complex roots using quadratic formula and square root method</li> <li>Rewrite quadratic equation in a factored form using its real and complex roots</li> <li>Counting multiplicities –quadratics having two roots in the complex numbers system</li> </ul>	
Resources	Amsco: p. 108-113	eMath: unit # 9 lesson #3 Engage NY:

• Lesson #4: The Discriminant and the Nature of the Roots

Standards	N-CN.C.7, A-REI.B.4b, A-APR.3, F-IF.8a MP 3 Construct viable argument and critique the reasoning of others, MP 7 Look for and make use of structure	
Objectives	<ul style="list-style-type: none"> <li>define and determine the value of the discriminant</li> <li>determine the nature of the roots using the discriminant</li> <li>Describe how finding discriminant relates to finding x-intercept of a parabola</li> <li>Construct viable argument and critique the reasoning of others</li> </ul>	



Resources	Amsco: p. 108 - 113	eMath: unit #9 lesson #4 Engage NY: Mod #1 Lesson #39

## Unit #5: Polynomial Functions and their Algebra

- Lesson #1: Long Division of Polynomials

Standards	A-APR.B.2, A-APR.6, A-APR.7, MP 6 Attend to precision	
Objectives	<ul style="list-style-type: none"> <li>Divide different degree polynomials by a binomial using long division</li> <li>Insert terms with zero as a coefficient for “missing powers”</li> <li>Using long division determine if a given binomial is a factor of a given polynomial</li> </ul>	
Resources	Amsco: p.138 – 141, Pearson: 304-306 Big Ideas: Chapter 4.3	eMath: Unit #10 Lesson #10 Engage NY: Mod #1 Lesson #18

- Lesson #2: Synthetic Division of Polynomials

Standards		
Objectives	<ul style="list-style-type: none"> <li>Dividing polynomials applying the method of synthetic division</li> </ul>	
Resources	Amsco: p.142 – 143 Big Ideas: Chapter 4.3	eMath: Engage NY:

- Lesson #3: Remainder and Factor Theorem

Standards	A-APR.D.6, A-APR.B.2	
Objectives	<ul style="list-style-type: none"> <li>Evaluating polynomial by the Remainder Theorem</li> <li>Determine if a given polynomial is divisible by a given binomial factor ( The Factor Theorem)</li> <li>Show how the Remainder theorem can help determine if a given number is the root of the polynomial. (NOTE: If <math>r</math> is a root of a polynomial then <math>x - r</math> is a factor of a polynomial</li> </ul>	
Resources	Amsco: 147 - 151	eMath: Unit #10 Lesson #11 Engage NY: Mod #1 Lesson #18, 19. See Lesson #20-21 for application of the Rem. Theorem

- Lesson #4 - 5: Finding Roots of Higher Degree Polynomial Equations

Standards	A-APR.B.3, N-CN.C.7, F-IF.7.C MP 6 Attend to precision, MP7 Look for and make sense of structure	
Objectives	<ul style="list-style-type: none"> <li>Test if a given number is the solution of a higher degree polynomial equation using the Remainder Theorem</li> <li>using Fundamental Theorem of Algebra state the number of zeros of a polynomial function</li> <li>solve a polynomial equation of 3<sup>rd</sup> degree given one of the factors and by applying synthetic division to find the remaining factors</li> <li>State the multiplicity of roots of a polynomial function</li> <li>Solve high order polynomials by factoring completely where some of the factors are complex numbers (Example: <math>x^4 - 3x^2 - 4 = 0</math> as <math>(x + i)(x - i)(x + 2)(x - 2)</math>)</li> </ul> <p>Next lesson</p> <ul style="list-style-type: none"> <li>State the difference between the solution(s) of the equation and x-intercepts (solutions</li> </ul>	

	may include complex numbers, x-intercepts are real solutions of the equation) <ul style="list-style-type: none"> <li>Construct a polynomial function in a factored form that has a specified set of zeros with stated multiplicity (including complex factors)</li> </ul> EXTENSION: Descartes' Rule of signs	
Resources	Amsco: p.152-154, 160-161 Pearson: 288-293, 296 Descartes' rule 165-167	eMath: unit # 10 lesson # See Engage NY: Mod #1 Lesson #11, 39

#### Lesson 5:

- Classify polynomials by degree
- Give an example of a quadratic equation with two distinct real solutions, one real solution, or two complex solutions
- Factor polynomial of the form  $(x^2 + a)$  as  $(x + ai)(x - ai)$   
( Example:  $x^2 + 9 = (x + 3i)(x - 3i)$ )
- Determine if a complex number is a solution to a given quadratic

- Lesson #6: Graphs and Zeros of a Polynomial Function.

Standards	F-IF.7.c, N-CN.9, A-APR.3 MP 5 Use appropriate tools strategically, MP 3 Construct a viable argument to critique the reason of others, MP 7 Look for and make use of structure	
Objectives	<ul style="list-style-type: none"> <li>Determine the number of real zeros, complex zeros, given the graph of a function and its equation</li> <li>Determine the degree of a polynomial function given its graph</li> <li>Create a sketch of higher degree polynomial function utilizing graphing calculator</li> <li>Critique reasoning of others</li> </ul> EXTENSION: determine degree of a polynomial by finding consecutive differences	
Resources	Amsco: p.154-164 Pearson: 280-287	eMath: unit # 10 lesson #2,3 See Engage NY: Mod #1 Lesson #14, 40

- Lesson #7: Even and Odd Degree Functions

Standards		
Objectives	<ul style="list-style-type: none"> <li>State characteristics of odd and even degree functions</li> <li>Identify the type of a given function based on a graph</li> <li>Investigate graphs of polynomial functions (the number of relative minima and maxima, increasing and decreasing intervals)</li> <li>Sketch polynomial functions using its properties</li> </ul>	
Resources	Amsco: p.52	eMath: Unit #7 Lesson #5 See Engage NY: Mod #1 Lesson #15

- Lesson #8: Structure in Graphs of Polynomial Functions

Standards		
Objectives	<ul style="list-style-type: none"> <li>Determine end behavior of polynomial functions by looking at the leading coefficient</li> <li>Match graphs of polynomial functions with their corresponding equations</li> <li>Find a polynomial function given its zeros or given its graph</li> <li>Use factored form of a polynomial function <u>to sketch</u> the components of its graph between zeros</li> </ul> EXTENSION: Real word application of polynomial function (create appropriate graphical representation)	

Resources	Amsco: p.159-164, Pearson 325	eMath: unit # lesson # See Engage NY:
-----------	-------------------------------	--

#### Unit #6: Rational Expressions and Equations

- Lesson #1: Simplifying Rational Expressions

Standards	A-APR.C.6, A-REI.A.2	
Objectives	<ul style="list-style-type: none"> <li>State which values will make the rational expression undefined</li> <li>State the domain of a rational function</li> <li>Reduce rational expressions to lowest terms</li> <li>Determine if the given two rational expressions are equivalent</li> </ul>	
Resources	Amsco: p. 185-187 Pearson: 527, 531	eMath: Unit #10 Lesson #6 See Engage NY: Mod #1 Lesson #22,23

- Lesson #2: Multiplying and Dividing Rational Expressions

Standards	Practice MP.7, A-APR.D.6	
Objectives	<ul style="list-style-type: none"> <li>Multiply and divide rational expressions and express them in a simplest form</li> <li>Simplify complex fractions by the process of dividing one rational expression by another</li> </ul>	
Resources	Amsco: p.187 – 192 Pearson: 528-533	eMath: Unit #10 Lesson #7 See Engage NY: Mod #1 Lesson #24

- Lesson #3: Adding and Subtracting Rational Expressions

Standards	Practice MP.7, A-APR.C.6	
Objectives	<ul style="list-style-type: none"> <li>Find a common multiple of the denominators to use as a common denominator</li> <li>Find equivalent rational expressions for each expressions using the common denominator</li> <li>Complete multistep problem involving adding, subtracting , multiplying, and dividing rational expressions</li> </ul>	
Resources	Amsco: p. 192 – 197 Pearson: 534 - 540	eMath: Unit #10 Lesson #8 See Engage NY: Mod #1 Lesson #

- Lesson #4: Complex Fractions

Standards		
Objectives	<ul style="list-style-type: none"> <li>Simplify complex fractions by the process of dividing one rational expression by another</li> </ul>	
Resources	Amsco: p.190, 192	eMath: Unit #10 Lesson #9 See Engage NY: Mod #1 Lesson #

- Lesson #5: Solving Rational Equations

Standards	A-REI.A.2, F-BF.B.4a, Practice MP.7	
Objectives	<ul style="list-style-type: none"> <li>Solve rational equations by cross-multiplying or multiplying each term by a common denominator</li> <li>Check for extraneous solutions</li> </ul> <p>EXTENSION: word problems leading to rational equations ( see Engage NY Mod #1 Lesson #27)</p>	
Resources	Amsco: p.197 – 204 Pearson: 542 - 547	eMath: Unit #10 Lesson #12 See Engage NY: Mod #1 Lesson #26

- Lesson #6: Solving word problems leading to rational equations

#### Unit #7: Powers and Radicals

- Lesson #1: Review of Integer Exponents

Standards		
Objectives	<ul style="list-style-type: none"> <li>Use appropriate laws of exponents to simplify expressions with positive, negative, and zero exponents</li> <li>Rewrite expressions using only positive exponents</li> </ul>	
Resources	Amsco: Pearson: 360	eMath: Unit #8 Lesson #3, Unit #4 Lesson #1 See Engage NY: Mod #1 Lesson #

- Lesson #2: Fractional Exponents

Standards	N-RN.A.1	
Objectives	<ul style="list-style-type: none"> <li>Simplify expressions including rational exponents</li> <li>Multiply and divide expressions with rational exponents</li> </ul> <p>EXTENSION: Irrational Exponents ( <math>2^{\sqrt{2}}</math>, <math>2^{\pi}</math> )</p>	
Resources	Amsco: p.241 Pearson: 381-387	eMath: Unit #4 Lesson #2 , Unit #8 Lesson #5 See Engage NY: Mod #1 Lesson #9

- Lesson #3: Properties of Exponents and Radicals

Standards	N-RN.A.2	
Objectives	<ul style="list-style-type: none"> <li>Rewrite expressions involving radicals in terms of rational exponents using the properties of exponents</li> <li>Simplify more complex expressions with radicals</li> </ul>	
Resources	Amsco: p.241 – 244, Pearson:363 -380	eMath: See Engage NY: Mod #1 Lesson #9

- Lesson #4: Simplifying Radical Expressions

Standards		
Objectives	<ul style="list-style-type: none"> <li>Simplify square roots and cubed roots with variables and exponents as radicands ( including negative radicands)</li> <li>Rationalize the denominator in a given expression</li> <li>Adding, multiplying, dividing radicals</li> </ul>	
Resources	Amsco: p.224 – 230, 237 -238 Pearson: 363 - 380	eMath: See Engage NY: Mod #1 Lesson #9,28

- Lesson #5: Solving Square Root Equations

Standards		
Objectives	<ul style="list-style-type: none"> <li>Solve radical equations and check for extraneous roots</li> <li>Justify the steps in solving radical equations</li> <li>Solving radical equations by moving one of the radicals to the opposite side of the equation and squaring both sides of the equation (<math>\sqrt{x-3} + \sqrt{x+4} = 4</math> and variations of it)</li> <li>Identify radical equations that do not have a solution</li> </ul>	
Resources	Amsco: p.245 – 250 Pearson: 390-396	eMath: Unit #8 Lesson #2 See Engage NY: Mod #1 Lesson #28,29

- Lesson #6: Solving Cube Root, Forth Root Equations, and Equations with Fractional Exponents

Standards		
Objectives	<ul style="list-style-type: none"> <li>Solve radical equations with higher index value by raising both sides of the equation to an appropriate power</li> <li>Solve equations with fractional exponents</li> </ul>	
Resources	Amsco: p.249, 257	eMath: Unit #4 Lesson #2 See Engage NY: Mod #1 Lesson #

- Lesson #7: Graphing Square Root and Cube Root Functions ( using calculator, and stating domain, range and translations)

Standards		
Objectives	<ul style="list-style-type: none"> <li>Graph square root and cube root functions using calculator</li> <li>Describe the characteristics of the above functions (domain, range, intervals of increase and decrease, end behavior)</li> <li>Sketch vertical and horizontal translations of the above functions</li> </ul>	
Resources	Amsco: p.251 – 255 Pearson: 414-420	eMath: Unit #8 Lesson #1 See Engage NY: Mod #1 Lesson #

## Unit #8: Sequences and Series

- Lesson #1 - 2: Review of Geometric and Arithmetic Sequences

Standards	F-BF.1.A	
Objectives	<ul style="list-style-type: none"> <li>Determine if a given sequence is arithmetic or geometric</li> <li>Write explicit equations of a given geometric (<math>a_n = a_1 r^{n-1}</math>) or arithmetic sequence (<math>a_n = a_1 + (n - 1)d</math>)</li> <li>Compare and contrast the explicit formula of two sequences</li> <li>Find the <math>n^{\text{th}}</math> term of an arithmetic or geometric sequence</li> </ul>	
Resources	Amsco: Pearson: 574-586 Big Ideas: Chapter 8.1, 8.2	eMath: Unit # Lesson # See Engage NY: Mod #1 Lesson #

- Lesson #3: Explicit and Recursive Formula for Geometric and Algebraic Sequences

Standards	F-BF.2, F-EF.8	
Objectives	<ul style="list-style-type: none"> <li>Write a recursive rule for given sequence of numbers (arithmetic and geometric)</li> <li>Apply recursive definition of arithmetic or geometric sequences to find several terms of a given sequence</li> <li>Translate a recursive rule into explicit equation and vice versa</li> </ul>	
Resources	Amsco: Pearson: 567-571 Big Ideas: Chapter 8.5	eMath: See Engage NY: Mod #1 Lesson #

- Lesson #4: Arithmetic and Geometric Series and Sigma Notation

Standards	F-BF.2, F-EF.8	
Objectives	<ul style="list-style-type: none"> <li>Compare and contrast sequences and series</li> <li>State the formula of a sum of Arithmetic and Geometric Series</li> <li>Find the sum of the first n terms of a given series</li> <li>Find sums using Sigma notation</li> </ul>	
Resources	Amsco: Pearson: 588-600	eMath:

	Big Ideas: Chapter 8.3, 8.4	See Engage NY: Mod #1 Lesson #
--	-----------------------------	--------------------------------

• Lesson #5: Geometric Series Application

Standards	F-LE.A.2, F-BF.1.A, F-BF.2	
Objectives	<ul style="list-style-type: none"> <li>• Write an explicit rule for the geometric sequence that models a real life problem and solve the problem</li> <li>• Given table of values that represents money earning scenario determine the rule needed to find money saved in 'n' weeks</li> <li>• Match recursive definition of geometric series with a real life scenario</li> </ul>	
Resources	Amsco: See IMG	eMath: See Engage NY: Mod #1 Lesson #

**SEE NEXT PAGE for MRS22 Overview**

## MRS22 Tentative Course Overview

### Unit #9: Exponential and Logarithmic Functions

- Lesson #1: Exponential Functions Basics (general form, determine if it is a growth or decay model based on a given equation or a graph)
- Lesson #2: Finding Equations of Exponential Functions (from a table or a graph, or coordinates of two points)
- Lesson #3: Solving Exponential Equations by Finding a Common Base
- Lesson #4: Modeling with Exponential Growth and Decay
- Lesson #5: Introduction to Logarithms
- Lesson #6: Graphs of Logarithmic Functions (including inverse relation between logarithmic and exponential functions)
- Lesson #7: Laws of Logarithms (possibly 2 days)
- Lesson #8: Natural and Base-10 Logarithms
- Lesson #9: Solving Logarithmic Equations
- Lesson #10: Solving Exponential Equations Using Logarithms
- Lesson #11: Compound Interest Problems

Unit #8	Sequences and Series
Total: 5 days	<ul style="list-style-type: none"><li>• Lesson #1 - 2: Review of Geometric and Algebraic Sequences</li><li>• Lesson #3: Explicit and Recursive Formula for Geometric and Algebraic Sequences</li><li>• Lesson #4: Arithmetic and Geometric Series and Sigma Notation</li><li>• Lesson #5: Geometric Series Application</li><li>• !!! NOTE: heavy emphasis on recursive definition of geometric sequence in the context of word problem. More days might be needed.</li></ul>

### Unit #10: Transformations of Functions

- Lesson #1: Shifting and Reflecting Functions (quadratic, exponential, square root functions, reference to notation  $a f(x - h) + k$ )
- Lesson #2: Key features of Different types of functions (domain, range, end behavior, increase/decrease, roots)
- Lesson #3: Rate of Change of Quadratic and Exponential Functions

### Unit #11: Circular Functions – Trigonometry

Consider starting with periodic functions intro Pearson: 828-834

- Lesson #1: Rotations and Angle Terminology
- Lesson #2: Radian Angle Measurement
- Lesson #3: The Unit Circle
- Lesson #4: The Definition of the Sine and Cosine Functions
- Lesson #5: Basic Graphs of Sine and Cosine
- Lesson #6: Vertical and Horizontal Shifting of Sinusoidal Graphs
- Lesson #7: The Frequency and Period of a Sinusoidal Graph
- Lesson #8: More Work with the Sine and Cosine Functions (trig identities)
- NOTE: ??? Can't find trig equations in the standards
- Lesson #9: Sinusoidal Modeling
- Lesson #10: The Tangent Function
- Lesson #11: The Reciprocal Function Pearson: 833-890

### Unit #12: Probability

- Lesson #1: Introduction to Probability
- Lesson #2: Sets and Probability

- Lesson #3: Adding Probabilities
- Lesson #4: Conditional Probability
- Lesson #5: Independent and Dependent Events
- Lesson #6: Multiplying Probabilities

#### Unit #13: Statistics

- Lesson #1: Variability and Sampling
- Lesson #2: Population Parameters
- Lesson #3 – The Normal Distributions
- Lesson #4 – The Normal Distribution and Z-Scores
- Lesson #5 – Sample Means
- Lesson #6 – Sample Proportions
- Lesson #7 – The Difference in Samples Means
- Lesson #8 – Linear Regression and Lines of Best Fit
- Lesson #9 – Other Types of Regression